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**AALBORG UNIVERSITY**  
DENMARK

## Lecture 3 - Experimental performance investigation of WECs

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# Experimental performance investigation of wave energy converters

# Guidelines and data sources ...

[www.iea-oceans.org](http://www.iea-oceans.org)

**ANNEX II**  
**Task 1.1 Generic and Site-related Wave Energy Data**  
**September 2010**

A report prepared by the RAMBOLL and LNEG to the OES-IA under the Annex II – Guidelines for Development and Testing of Ocean Energy Systems  
September 2010  
OES-IA Document n° TD2-1.1



RAMBOLL

IEA | OES  
Ocean Energy Systems

ment on Ocean Energy Systems  
y Agency

**WAVE DATA CATALOGUE  
FOR RESOURCE ASSESSMENT  
IN IEA-OES MEMBER COUNTRIES**

March 2009

A report prepared by INETI to the IEA-OES under  
**ANNEX I - Review, Exchange and Dissemination  
of Information on Ocean Energy Systems**

IEA-OES Document No: T0103

INETI

IEA | OES  
Ocean Energy Systems



Equitable Testing and Evaluation of Marine Energy Extraction  
Devices in terms of Performance, Cost and Environmental Impact  
Grant agreement number: 213380

**EquiMar**

Deliverable D2.2  
Wave and Tidal Resource Characterisation

<https://www.wiki.ed.ac.uk/display/EquiMarwiki/EquiMar>



International  
Electrotechnical  
Commission

**TC 114**

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International Standards and Conformity Assessment  
for all electrical, electronic and related technologies

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Standards development > How we work > Technical Committees & Subcommittees > **TC 114 Dashboard**

**TC 114** Marine energy - Wave, tidal and other water current converters

Scope | **Structure** | Projects / Publications | Documents | Meetings

**TC 114 Scope**

To prepare international standards for marine energy conversion systems. The primary focus will be on conversion of wave, tidal and other water current energy into electrical energy, although other conversion methods, systems and products are included. Tidal barrage and dam installations, as covered by TC 4, are excluded. The standards produced by TC 114 will address: \* system definition \* performance measurement of wave, tidal and water current energy converters \* resource assessment requirements, design and survivability \* safety requirements \* power quality \* manufacturing and factory testing \* evaluation and mitigation of environmental impacts



**Further information**

Secretariat | [United Kingdom](#)

Strategic Business Plan | [Download](#)

**Tools (members only)**

- Collaboration Tools**  
Access restricted to TC 114 members only
- Document open for vote/comment**

# **IECTC 114 – National ‘mirror’ committee (DK: DS S-614)**

**Member based, DK:**

- **Aalborg Universitet**
- **Wave Star Energy A/S**
- **Bølgekraftforeningen**
- **Sterndorff Engineering**

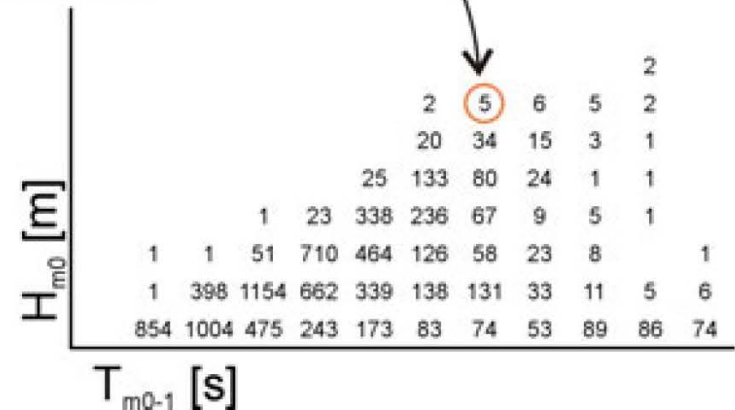
<b>PT 62600-1:</b>	<b>Terminology.</b>
<b>PT 62600-2:</b>	<b>Design requirements for marine energy systems.</b>
<b>PT 62600-10:</b>	<b>Assessment of mooring system for marine energy converters.</b>
<b>PT 62600-20:</b>	Guideline for design assessment of Ocean Thermal Energy Conversion (OTEC) system.
<b>PT 62600-30:</b>	Electrical power quality requirements for wave, tidal and other water current energy converters.
<b>PT 62600-40:</b>	Acoustic characterization of marine energy converters.
<b>PT 62600-100:</b>	<b>Power performance assessment of electricity producing wave energy converters.</b>
<b>PT 62600-101:</b>	<b>Wave energy resource assessment and characterization.</b>
<b>PT 62600-102:</b>	<b>Wave Energy Converter Power Performance Assessment at a Second Location Using Measured Assessment Data.</b>
<b>PT 62600-103:</b>	<b>Wave Tank Testing of Wave Energy Converters.</b>
<b>PT 62600-200:</b>	Power performance assessment of electricity producing tidal energy converters.
<b>PT 62600-201:</b>	Tidal energy resource assessment and characterization.
<b>PT 62600-202:</b>	Scale testing of tidal stream energy systems.
<b>PT 62600-300:</b>	Electricity producing river energy converters - Power performance assessment.
<b>PT 62600-301:</b>	River energy resource assessment and characterization.

# Establish distribution of prevailing wave conditions

- Sources
  - direct measurements
  - hindcast from wind
  - models, transformation to location
- Parameters
  - significant wave heights
  - peak / energy / average periods
  - wave energy contents
  - direction
  - probability
- Amount of data
  - 20-30 years would be nice to have reliable estimation of average production, but...
  - normally not available directly for location
  - transformation necessary
  - check against shorter term wave measurements

+1

## Resultant power spectrum for a single sea state



Ph. D. course: Modeling and Control of Wave Energy Converters

# Modeling of wave conditions for energy production

North Sea, Danish Sector (150 km offshore, d= 50 m)

T02 Hm0	2.0 - 3.0	3.0 - 4.0	4.0 - 5.0	5.0 - 6.0	6.0 - 7.0	7.0 - 8.0	8.0 - 9.0	9.0 - 10.0	10.0 - 11.0	11.0 - 12.0	12.0 - 13.0	Sum	%
0.00 - 0.50	460.3	415.2	66.9	19.4	4.6	0.6	0.1					967.1	11.0
0.50 - 1.00	51.9	1520.2	542.4	136.3	46.3	13.8	3.8	0.9	1.9			2317.5	26.4
1.00 - 1.50		239.7	1349.3	138.6	32.5	13.3	6.7	2.4	2.3	0.1		1784.9	20.4
1.50 - 2.00		0.6	689.3	448.5	11.5	3.7	2.1	0.7	0.8	0.4		1157.6	13.2
2.00 - 2.50			20.3	780.8	20.5	1	0.4	0.1	0.1	0.4	0.3	823.9	9.4
2.50 - 3.00			0.4	338.2	214.1	0.3	0.1					553.1	6.3
3.00 - 3.50				17	372.5	1.2						390.7	4.5
3.50 - 4.00				0.3	230.9	34.5						265.7	3.0
4.00 - 4.50					23.7	154.4	0.1					178.2	2.0
4.50 - 5.00					1.2	130.4	0.3					131.9	1.5
5.00 - 5.50						58	21.1					79.1	0.9
5.50 - 6.00						3.8	46.7					50.5	0.6
6.00 - 6.50						0.3	26.7					27	0.3
6.50 - 7.00							15.5	1.9				17.4	0.2
7.00 - 7.50							2	7.3				9.3	0.1
7.50 - 8.00							0.1	6.6				6.7	0.1
8.00 - 8.50								3.1				3.1	0.0
8.50 - 9.00								1.3	0.1			1.4	0.0
9.00 - 9.50								0.1	0.3			0.4	0.0
Sum	512.2	2175.7	2668.6	1879.1	957.8	415.3	125.7	24.4	5.5	0.9	0.3	8765.5	100.0
%	5.8	24.8	30.4	21.4	10.9	4.7	1.4	0.3	0.1	0.0	0.0	100.0	



# Modeling of wave conditions for energy production

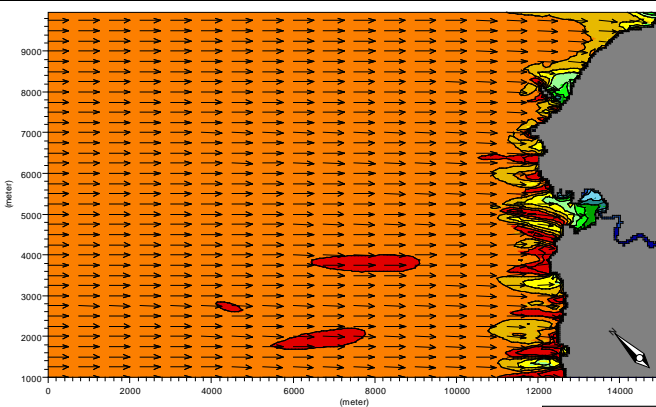
North Sea, Danish Sector (150 km offshore, d= 50 m)

T02	2.0	3.0	4.0	5.0	6.0	7.0	8.0	9.0	10.0	11.0	12.0	Sum	%
Hm0	-	-	-	-	-	-	-	-	-	-	-		
	3.0	4.0	5.0	6.0	7.0	8.0	9.0	10.0	11.0	12.0	13.0		
0.00 - 0.50	460.3	415.2	66.9	19.4	4.6	0.6	0.1					967.1	11.0
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						58	21.1					79.1	0.9
						3.8	46.7					50.5	0.6
						0.3	26.7					27	0.3
							15.5	1.9				17.4	0.2
							2	7.3				9.3	0.1
							0.1	6.6				6.7	0.1
								3.1				3.1	0.0
								1.3	0.1			1.4	0.0
								0.1	0.3			0.4	0.0
Sum	512.2	2175.7	2006.0	1679.1	957.6	415.3	125.7	24.4	5.5	0.9	0.3	8765.5	100.0
%	5.8	24.8	30.4	21.4	10.9	4.7	1.4	0.3	0.1	0.0	0.0	100.0	

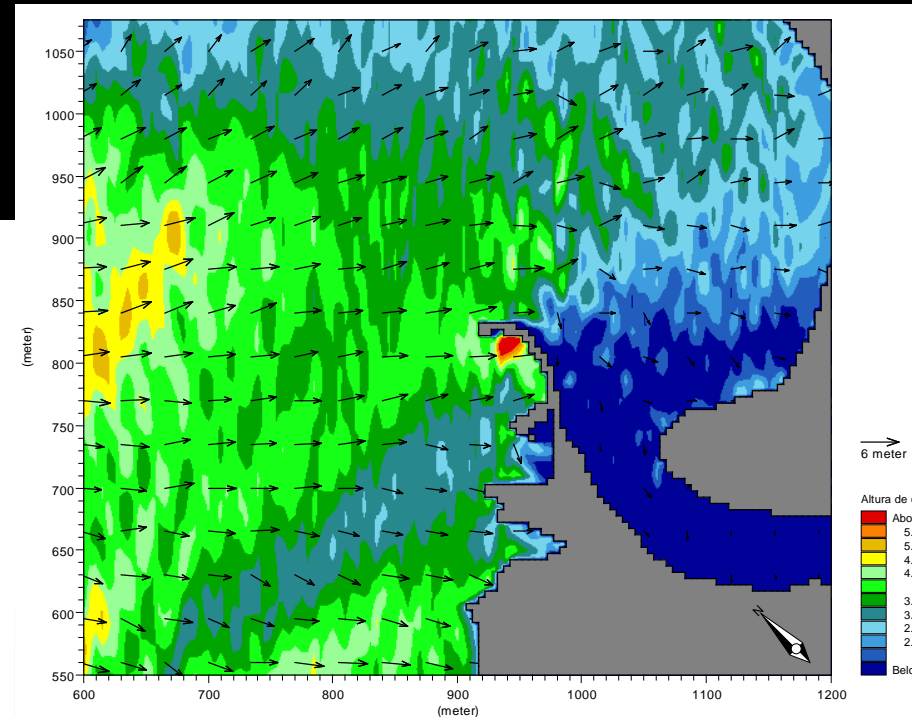
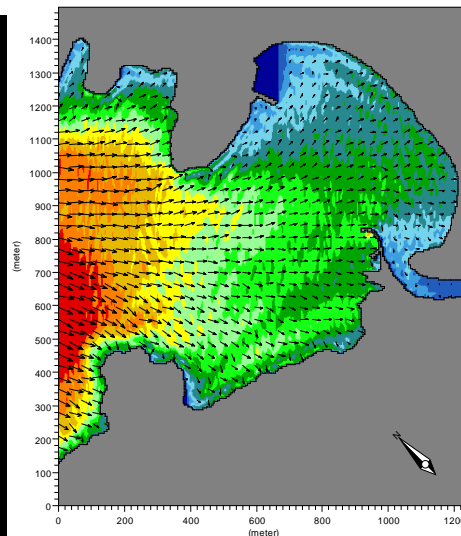


# Transformation of waves from offshore to near/onshore

## Numerical wave transformation modelling



- WAN – deep water / SWAN - shallow water
- MIKE21 Model
- WAVEWATCH III
- MILDwave
- Tomawac



# Design waves

## Extreme conditions

- 50 years event often used (corresponding to a 2 % exceedence probability pr. year)
- In phase 1 tests often only qualitative observations used
- In phase 2 extreme conditions are reproduced using 1-2.000 waves. Dimensioning load often taken as F1/250

## Fatigue

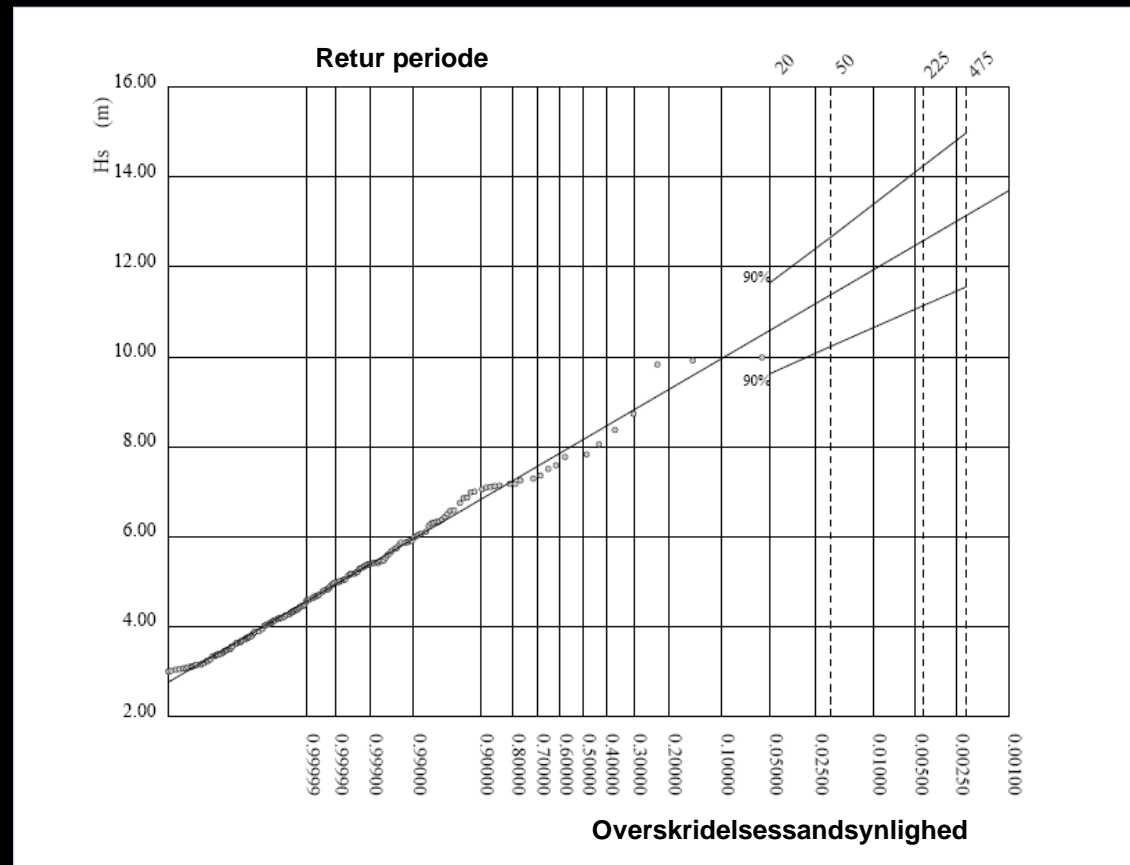
- Often not considered at phase 1 and 2

### North Sea, Danish Sector

Sea State	Hs	Tz	Tp	Return Period
	<i>m</i>	<i>sec</i>	<i>sec</i>	<i>years</i>
D10	8.0	9.4	13.1	10
D50	9.0	9.9	13.8	50
D100	10.0	10.4	14.5	100

Sea state	1	2	3	4	5	
Hs (m)	1	2	3	4	5	6-10
H (m)	0.7	1.4	2.1	2.8	3.5	4.2-7.1
N [·10 <sup>4</sup> ]	450	170	71	25	7.5	2.0

# Statistics of extreme events



Again – wave transformation might be necessary

# How to get performance data?

- The straight way is full scale experience... normally not an option!
- We need model testing and/or numerical modelling

## What is a physical model?

- A physical system reproduced (at reduced size) so dominant forces are represented in the model in correct proportion to the prototype

# Why model tests?

- Seek qualitative insight
- Obtain measurements to check theoretical results
- Obtain measurements to validate/calibrate numerical results
- Obtain measurements of phenomena too complicated for theoretical/numerical evaluation

# Dimensional analysis

- Dimensional analysis is a rational procedure for combining physical variables into dimensionless products, and thereby reducing the number of variables that need to be considered.
- Steps:
  - 1. Identify independent variables
  - 2. Select dependent variable
  - 3. Establish possible independent dimensionless products
  - 4. Reduce system var. to the proper number of independent dimensionless variables

# Buckingham Pi theorem

“In a dimensionally homogeneous equation involving 'n' variables, the number of dimensionless products that can be formed from 'n' variables is 'n-r', where 'r' is the number of fundamental dimensions (L T M) encompassed by the variables”

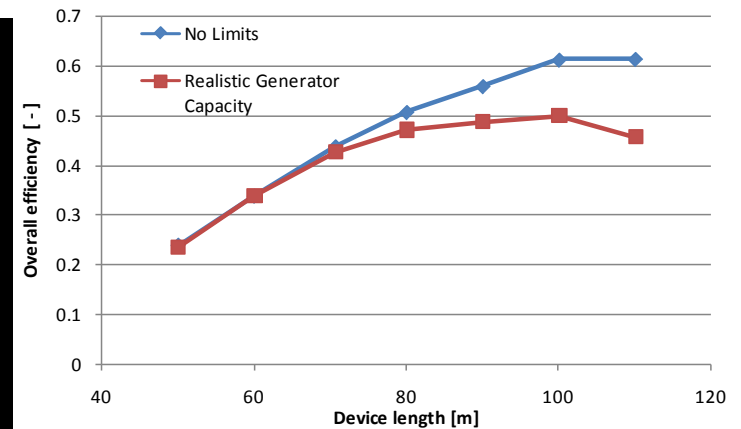
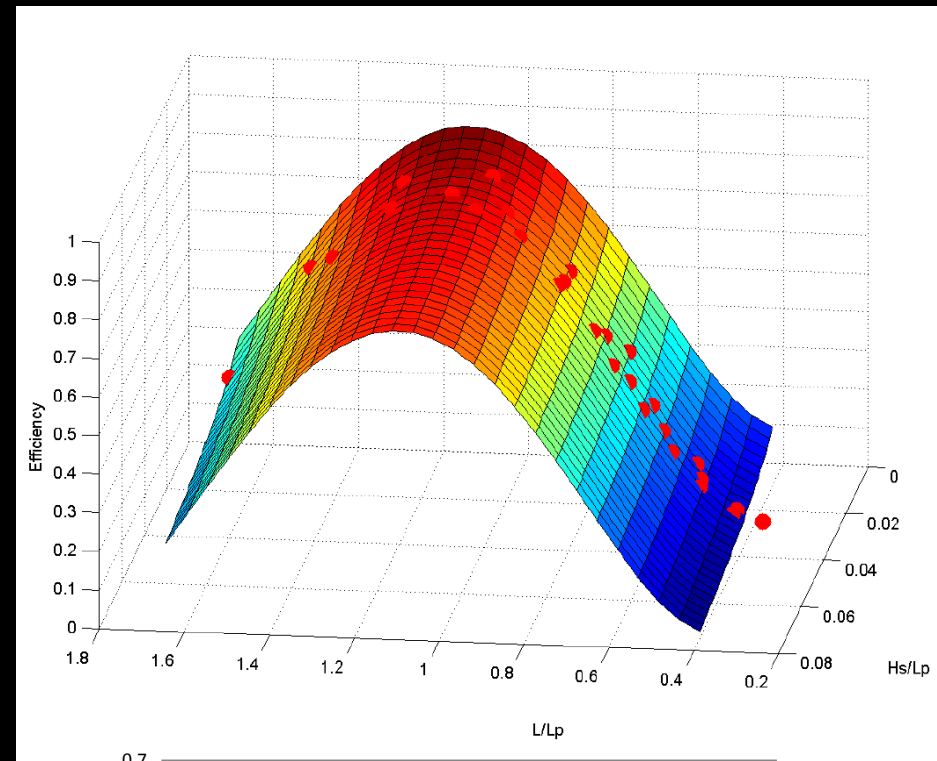
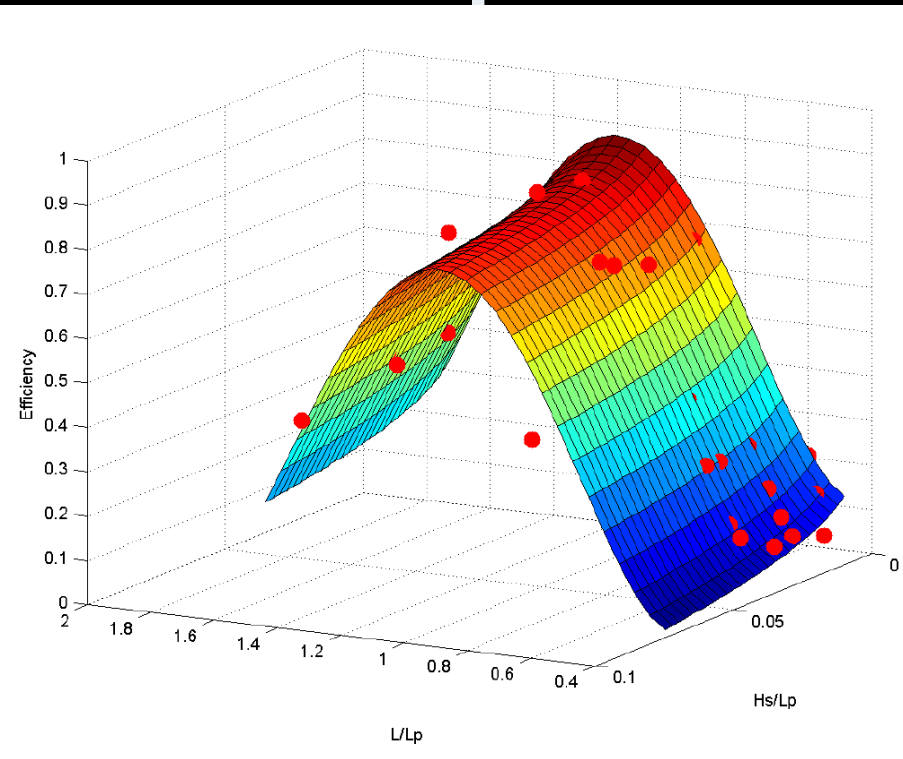
$$x_1 = f(x_2, x_3, \dots, x_n)$$
$$\Downarrow$$
$$\Pi_1 = \Psi(\Pi_2, \Pi_3, \dots, \Pi_{n-r})$$

if all original variables appear at least once in one of the dimensionless products

Physical model tests can then be used to establish correlations between these dimensionproducts



# An example



# Principles of similitude – scaling laws

- To ensure similitude between prototype and model, the following requirements must be met:
  - Geometric similarity – ratio between dimensions constant [L]
  - Kinematic similarity – ratio between motions constant [L T]
  - Dynamic similarity – ratio between forces constant [L T M]
- Impossible for ALL forces. Evaluation of violations necessary – these are the scale effects.

# Scaling criteria

- Froude – gravity
- Reynolds – viscous
- Weber – surface tension
- Gauchy – elasticity
- Euler – pressure coef.

Characteristic	Dimension	Froude	Reynolds
Geometric			
Length	$[L]$	$N_L$	$N_L$
Area	$[L^2]$	$N_L^2$	$N_L^2$
Volume	$[L^3]$	$N_L^3$	$N_L^3$
Kinematic			
Time	$[T]$	$N_L^{1/2} N_\rho^{1/2} N_\gamma^{-1/2}$	$N_L^2 N_\rho N_\mu^{-1}$
Velocity	$[LT^{-1}]$	$N_L^{1/2} N_\rho^{-1/2} N_\gamma^{1/2}$	$N_L^{-1} N_\rho^{-1} N_\mu$
Acceleration	$[LT^{-2}]$	$N_\gamma N_\rho^{-1}$	$N_L^{-3} N_\rho^{-2} N_\mu^2$
Discharge	$[L^3 T^{-1}]$	$N_L^{3/2} N_\rho^{-1/2} N_\gamma^{1/2}$	$N_L N_\rho^{-1} N_\mu$
Kinematic Viscosity	$[L^2 T^{-1}]$	$N_L^{3/2} N_\rho^{-1/2} N_\gamma^{1/2}$	$N_\rho^{-1} N_\mu$
Dynamic			
Mass	$[M]$	$N_L^3 N_\rho$	$N_L^3 N_\rho$
Force	$[MLT^{-2}]$	$N_L^3 N_\gamma$	$N_\rho^{-1} N_\mu^2$
Mass Density	$[ML^{-3}]$	$N_\rho$	$N_\rho$
Specific Weight	$[ML^{-2}T^{-2}]$	$N_\gamma$	$N_L^{-3} N_\rho^{-1} N_\mu^2$
Dynamic Viscosity	$[ML^{-1}T^{-1}]$	$N_L^{3/2} N_\rho^{1/2} N_\gamma^{1/2}$	$N_\rho$
Surface Tension	$[MT^{-2}]$	$N_L^2 N_\gamma$	$N_L^{-1} N_\rho^{-1} N_\mu^2$
Volume Elasticity	$[ML^{-1}T^{-2}]$	$N_L N_\gamma$	$N_L^{-2} N_\rho^{-1} N_\mu^2$
Pressure and Stress	$[ML^{-1}T^{-2}]$	$N_L N_\gamma$	$N_L^{-2} N_\rho^{-1} N_\mu^2$
Momentum, Impulse	$[MLT^{-1}]$	$N_L^{7/2} N_\rho^{1/2} N_\gamma^{1/2}$	$N_L^2 N_\mu$
Energy, Work	$[ML^2T^{-2}]$	$N_L^4 N_\gamma$	$N_L N_\rho^{-1} N_\mu^2$
Power	$[ML^2T^{-3}]$	$N_L^{7/2} N_\rho^{-1/2} N_\gamma^{3/2}$	$N_L^{-1} N_\rho^{-2} N_\mu^3$

# Model laws and scaling

Froudes Model law:

- Inertia forces are dominating. These are proportional to the volume/mass of the device.
- Friction forces are negligible.
- Geometrical similar with full scale device.

Choice of scaling ratio:

- Measuring accuracy  $\Rightarrow$  model size  $\uparrow$
- Ratio between friction and inertia forces  $\Rightarrow$  model size  $\uparrow$
- Surface tension  $\Rightarrow$  model size  $\uparrow$
- Modelling of PTO system  $\Rightarrow$  model size  $\uparrow$
- Handability  $\Rightarrow$  model size  $\downarrow$
- Time restrictions  $\Rightarrow$  model size  $\downarrow$
- Available laboratory size  $\Rightarrow$  model size  $\downarrow$
- Economics  $\Rightarrow$  model size  $\downarrow$

Parameter	Model	Full Scale	Example 1:100
Length	1	S	100
Area	1	$S^2$	10000
Volume	1	$S^3$	1000000
Time	1	$S^{0.5}$	10
Velocity	1	$S^{0.5}$	10
Force	1	$S^3$	1000000
Power	1	$S^{3.5}$	10000000

$\Rightarrow$  Scaling ratios of 1:25 – 40 often used in our lab. (1 W ~ 80 – 400 kW !!!)

# Measuring techniques – an overview

Measurements of:

- waves (surface elevations)
- pressures
- Forces (strain / stress)
- Motions (displacements / velocity / accelerations)
- Flow
- Torque
- Current velocity
- Dimensions
- \*\*\*



# Wave (surface elevation) measurements

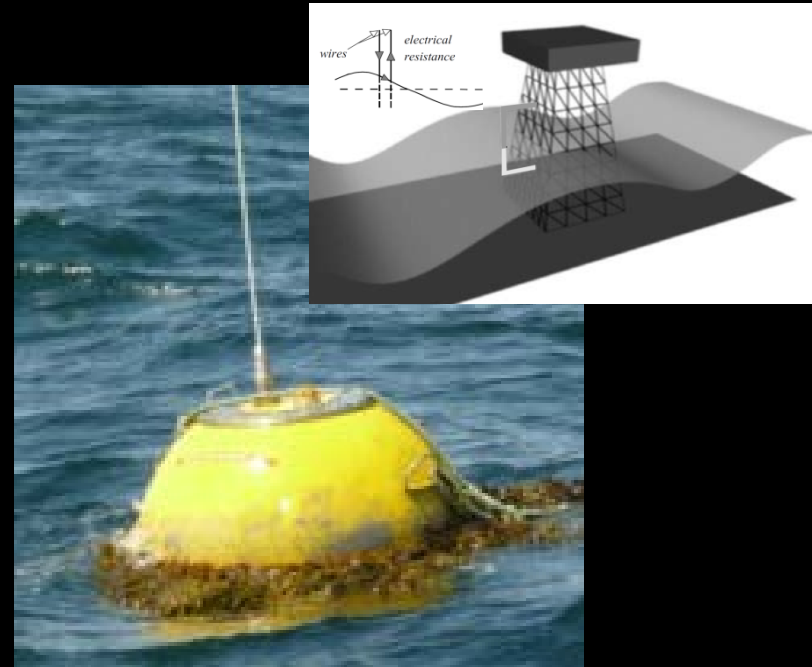
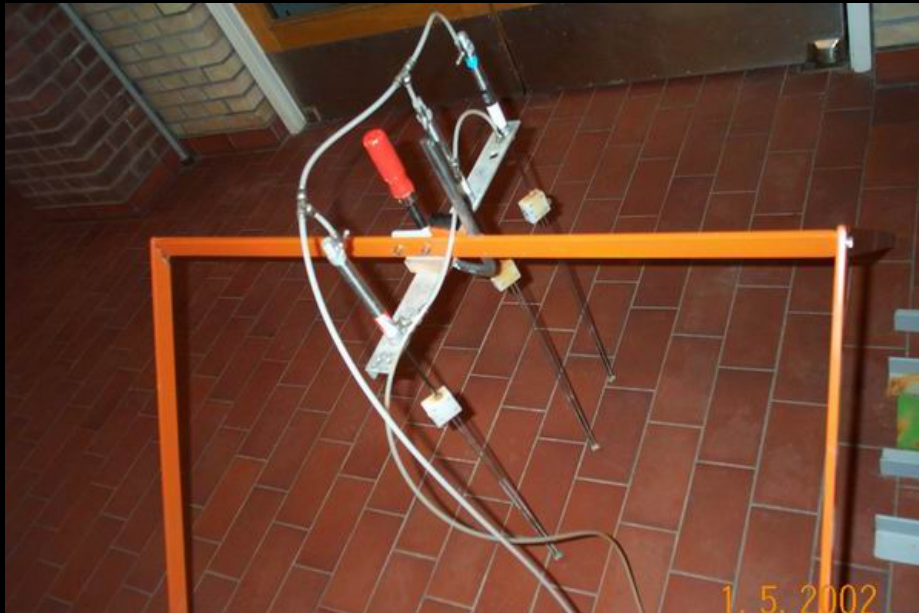
## Resistance gauge

- Lab., also for run-up

## Capacitance gauge

- Sea water ok

- 3D arrays
  - for 3D wave analysis
- Wave rider buoy
  - Point or 3D wave data



# Wave (surface elevation) measurements

## ADCP

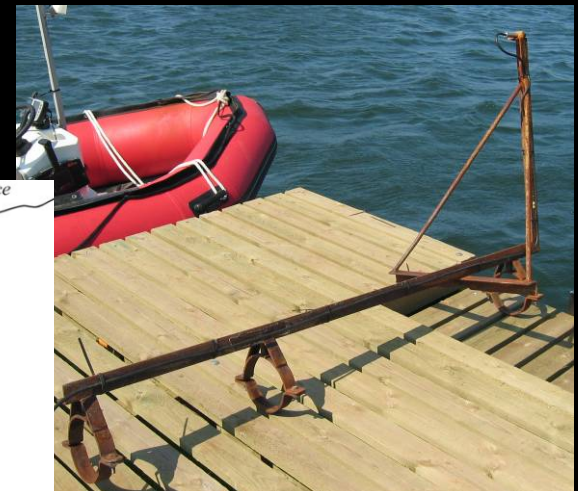
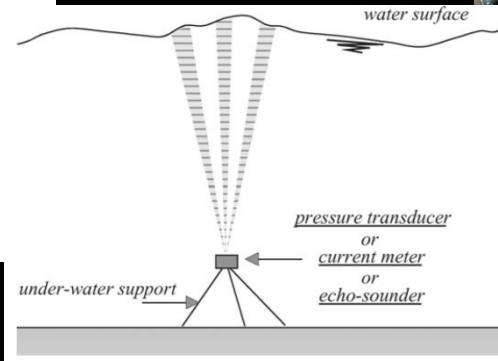
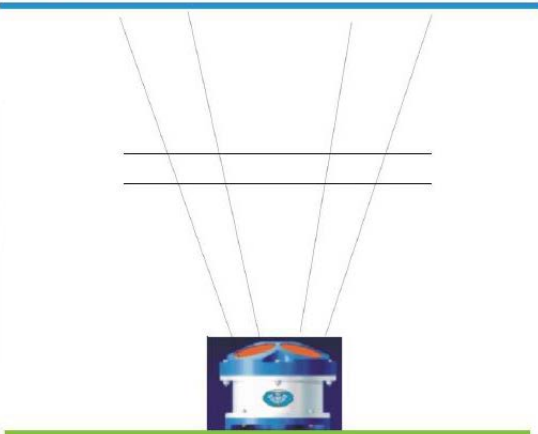
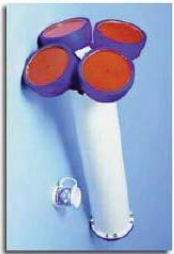
- Sea, also 3D data

## Radar

- Sea, point, need structure

- Step gauge
  - Lab. or sea, good for run-up
- Pressure transducer
  - Primarely sea, cheap, data needs transformation

## Acoustic Doppler Current Profiler

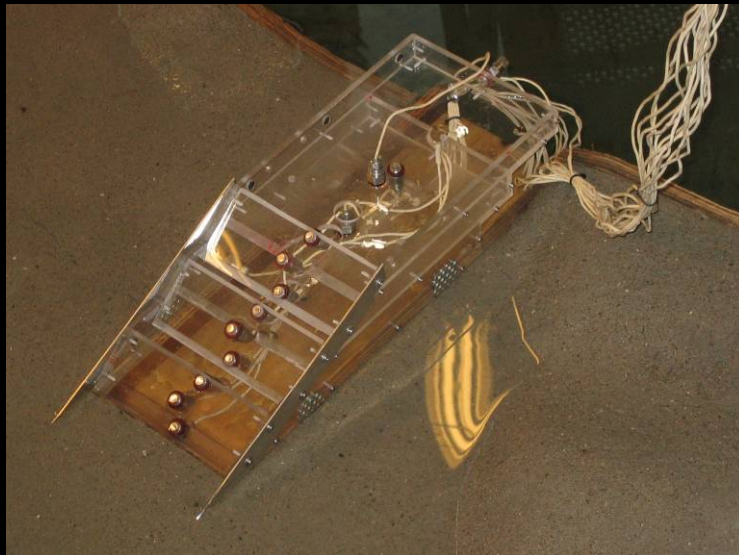




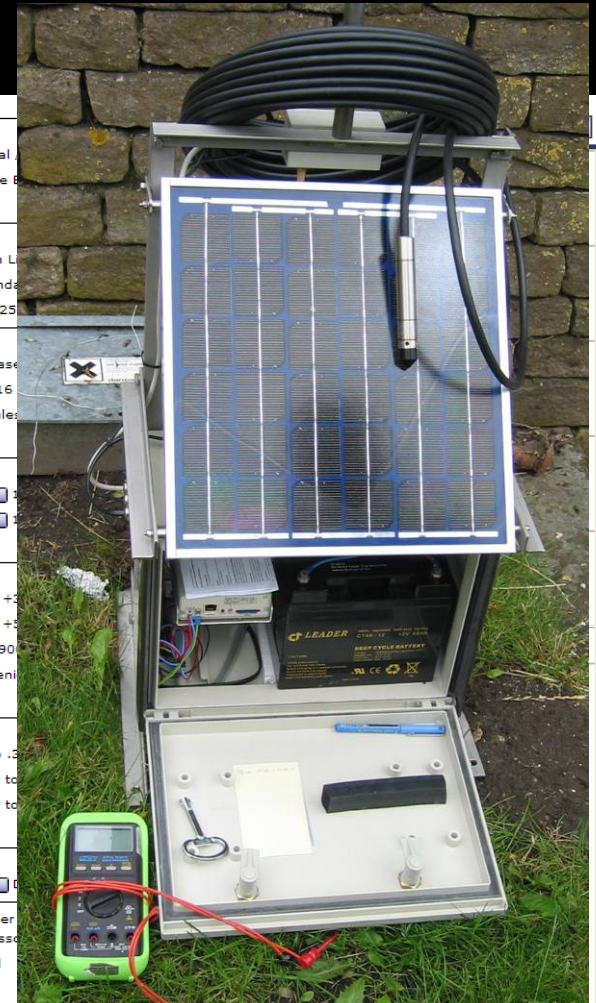
# Pressure Measurements

Pressure transducers /  
transmitters

- Lab and real sea
- Various sizes shapes

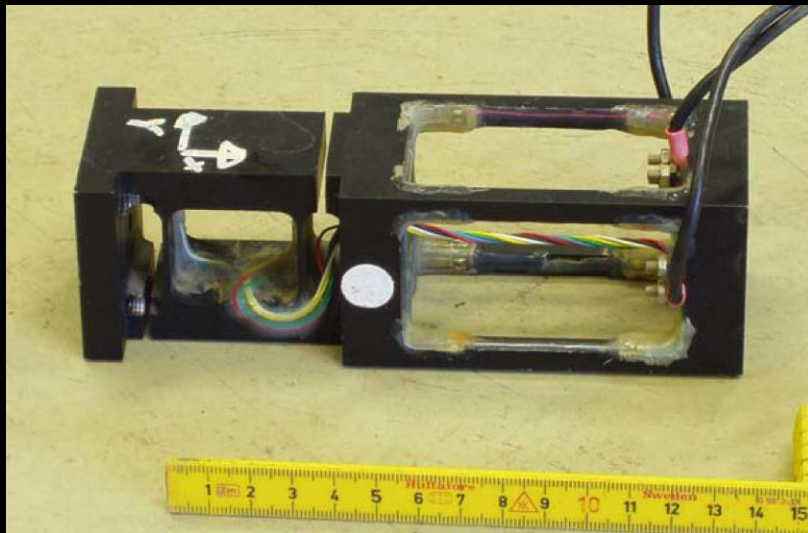


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<input type="checkbox"/> Flight Test & Instrumentation	<input type="checkbox"/> Resource B
<input type="checkbox"/> Blast Testing	
<b>Size:</b>	
<input type="checkbox"/> Cylindrical Probes	<input type="checkbox"/> Thin L
<input type="checkbox"/> Miniature Threaded	<input type="checkbox"/> Stand
<input type="checkbox"/> Less than 1" (25.4mm) Diameter	<input type="checkbox"/> 1" (25
<b>Media:</b>	
<input type="checkbox"/> All nonconductive, noncorrosive liquids or gas	
<input type="checkbox"/> Any liquid or gas compatible with 15-5 or 316	
<input type="checkbox"/> Any liquid or gas compatible with 15-5 stainless	
<input type="checkbox"/> Others	
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<input type="checkbox"/> 28 ± 4	<input type="checkbox"/> 24 ± 4
<input type="checkbox"/> 5 V	<input type="checkbox"/> 10 V
<input type="checkbox"/> Other	<input checked="" type="checkbox"/> 4-20mA Output Available
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<input type="checkbox"/> -65 to +250°F (-55 to +120°C)	<input type="checkbox"/> -65 to +3
<input type="checkbox"/> -65 to +450°F (-55 to +235°C)	<input type="checkbox"/> -65 to +5
<input type="checkbox"/> -65 to +750°F (-55 to +400°C)	<input type="checkbox"/> Up to 90
<input type="checkbox"/> Over 1000°F (538°C)	<input type="checkbox"/> Cryogeni
<input type="checkbox"/> Other	
<b>Pressure Range:</b>	
<input type="checkbox"/> Microphone	<input type="checkbox"/> 0-5 PSI (0 to .3
<input type="checkbox"/> 0-15 PSI (0 to 1.0 BAR)	<input type="checkbox"/> 0-100 PSI (0 to
<input type="checkbox"/> 0-250 PSI (0 to 17 BAR)	<input type="checkbox"/> 0-500 PSI (0 to
<input type="checkbox"/> High Pressure	
<b>Operational Mode:</b>	
<input type="checkbox"/> Absolute	<input type="checkbox"/> Gage
<input type="checkbox"/> Sealed Gage	<input type="checkbox"/> S
<b>Special Products:</b> Selecting these may cancel other	
<input type="checkbox"/> Acceleration Compensated	<input type="checkbox"/> Microprocess
<input type="checkbox"/> Pressure / Temperature	<input type="checkbox"/> Water Cooled
<input type="checkbox"/> Load / Soil Dynamics	



# Forces (strain / stress) - laboratory

- Frame with displacement gauge
- "Bone" with SG's
- Tension/compression transducer
- SG's on structure
- Real sea: Mechanical protection!
- Quarter/half/full bridge configuration





# Forces (strain / stress) - sea

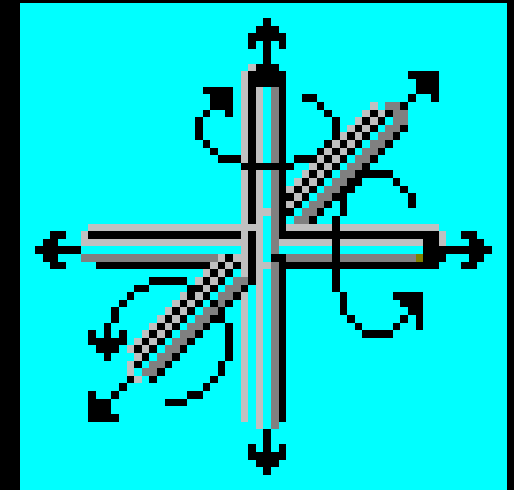
- Tension/compression transducer
- SG's on structure



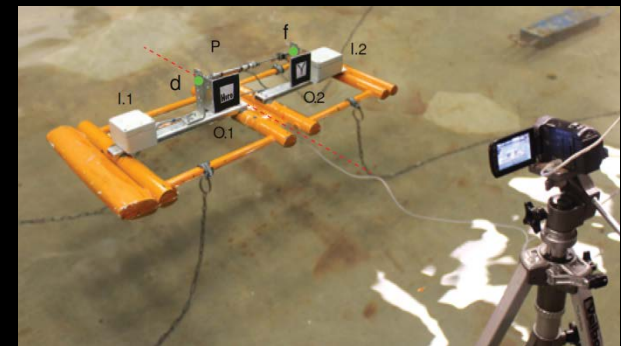
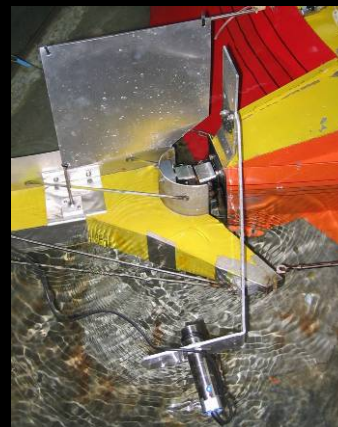
# Motions (displacements / velocity / accelerations)

## 6 DOF rigid body motions

- Translation: Heave, surge, sway
- Rotation: Pitch, roll, yaw



- Wire / potentiometer
- Ultrasonic/laser remote sensing
- Camera based sensing
- Accelerometers (IMUs)

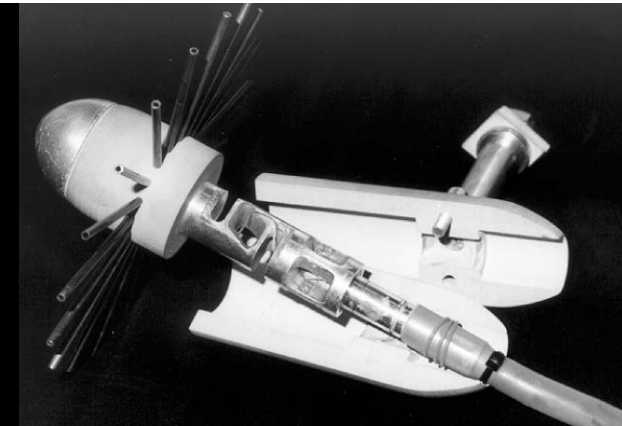
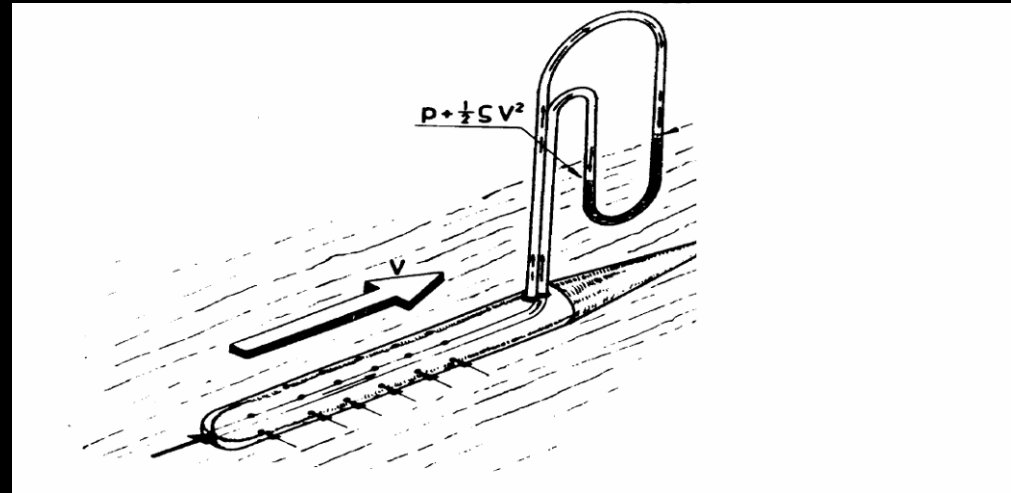




# Flow

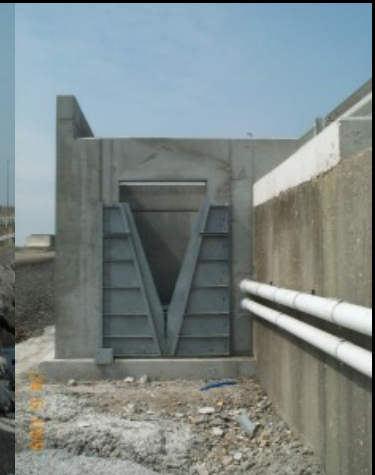
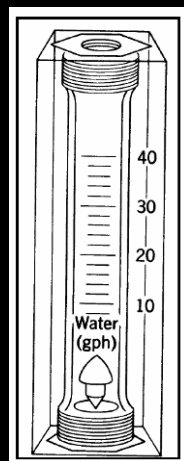
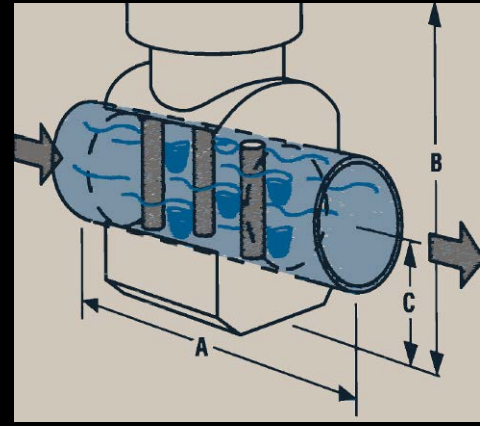
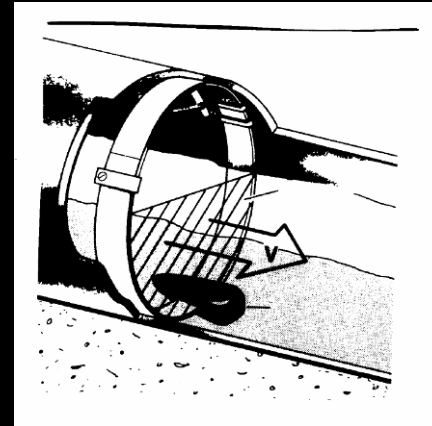
$$P = Q(\frac{1}{2}\rho v^2 + \rho gh + \Delta p)$$

- Ultrasonic (Doppler)
- Pitot pipe
- Turbine flow meter
- Pressure and moment



# Flow

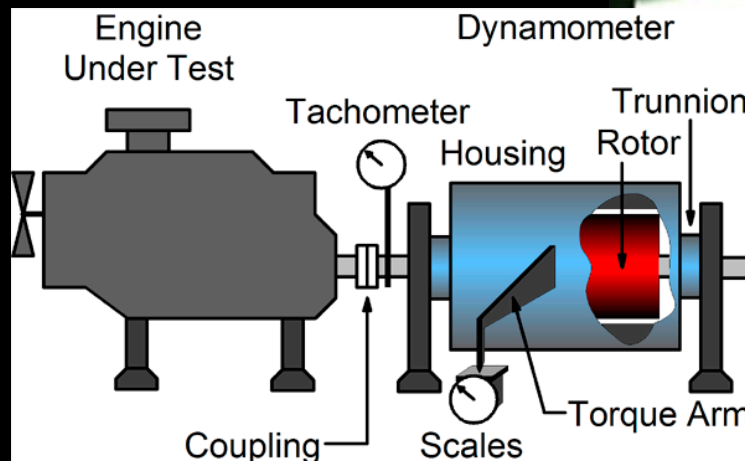
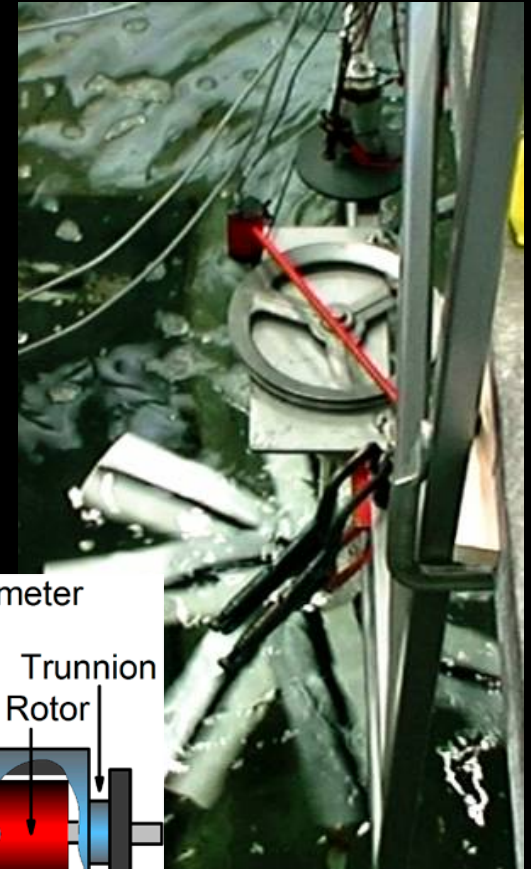
- Electromagnetic field
- Rotameter
- Vortex flow meter
- Head loss over orifice
- Flow over vier
- Filling of container, measuring weight or water level





# Torque – loading control

- Water breaks
- Disc brakes
- Dynamometer
- Weight in string on axle
- Generator





# Modeling the power take-off system

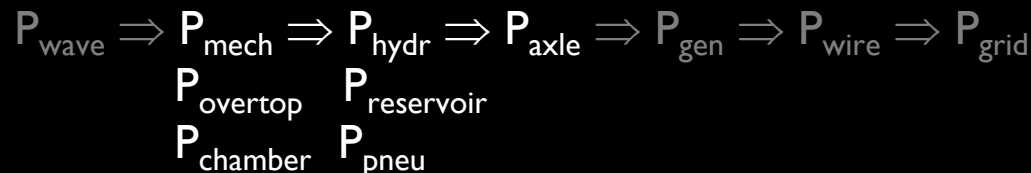
## Challenges

- Scaling the PTO normally does not follow the Froud scaling laws. Therefore, a direct model of the full scale PTO can not be used
- The load from the PTO feeds back to the hydraulic behavior of the device, and is normally of paramount importance for the performance of the device. Therefore, the load from the PTO on the system have to be controllable

## Solutions

- In smaller scale, "just" model the loading from the PTO
- Measure the power production early in the power chain

Bevare of where in the chain of power you are measuring!



# Some examples – weights lifted by rotating axle

Power measured through weight, axle diameter, displacement and time

## Pros

- Very simple and direct measurement. Easy to change loading – weights and/or axle diameter

## Cons

- Limited test durations – need large heights for long tests. Therefore best for regular wave tests
- Not possible to change loading "on the fly"
- Gives a constant torque on axle – not realistic loading characteristic of a generator



# Some examples – friction force and velocity

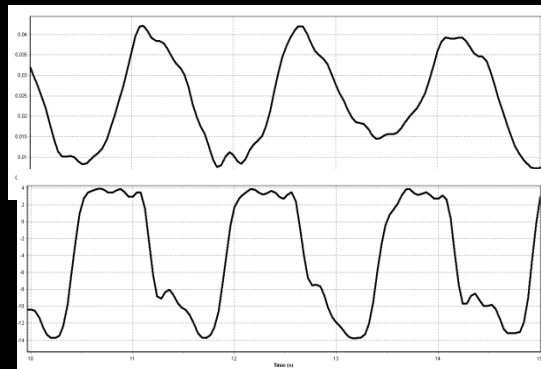
Power measured through force and displacement time series

## Pros

- No limitations on test duration
- Loading can in principle be changed "on the fly"

## Cons

- Risk of changing load characteristics due to heating of brakes
- Sometimes hard to get little enough friction for small waves





# Some examples – air flow

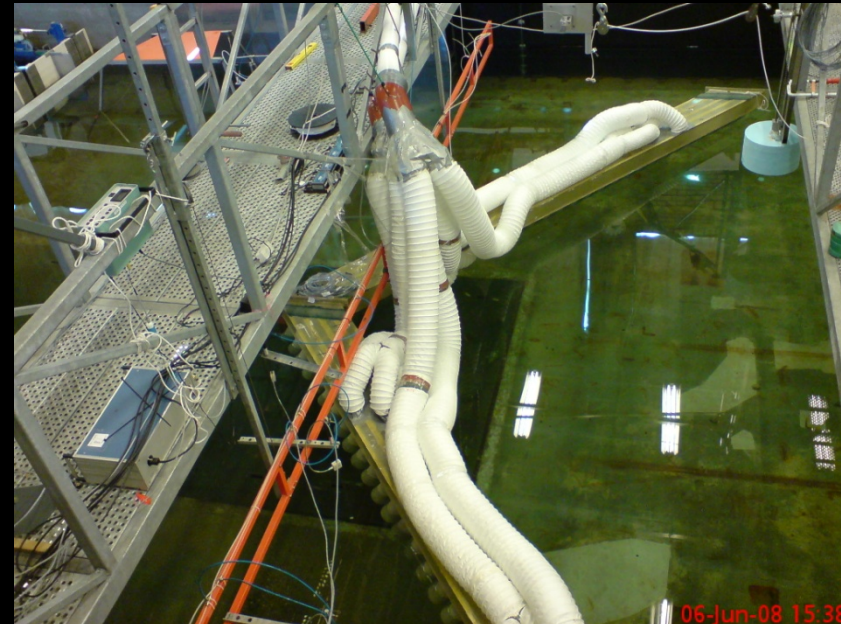
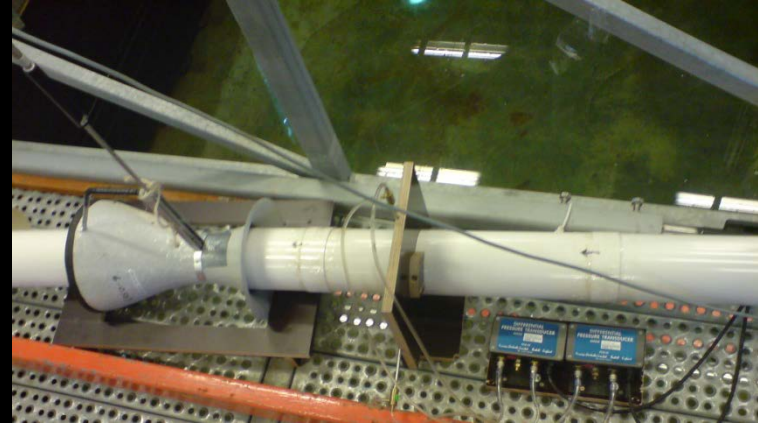
Power measured through flow and pressure time series

## Pros

- Most appropriate for OWCs to get power measurements as early in the power chain as possible

## Cons

- Difficulties in measuring fluctuating air flows



# Some examples – overtopping flow

Power production measured through crest height and overtopping flow time series

## Pros

- Simple and direct measurement
- Easy to change loading – crest height
- Power obtained very early in the power chain

## Cons

- Resolution of flow in time
- Not possible to change loading "on the fly"
- Power obtained very early in the power chain



# Some examples – Controllable force and velocity

Power production measured through force and velocity time series

## Pros

- Full control – can be run in force or displacement control mode

## Cons

- Cost
- Complexity





# Some examples – Controllable torque and rotational speed

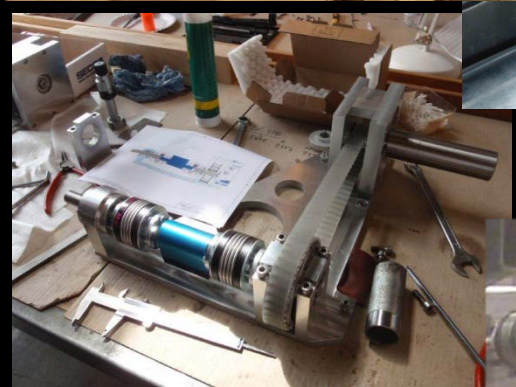
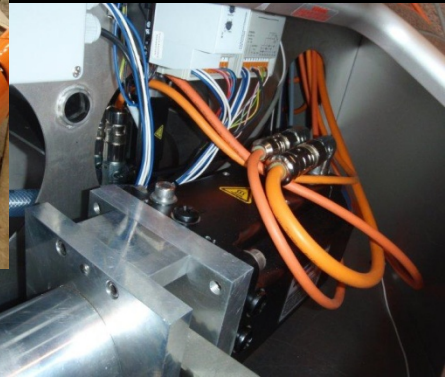
Power production measured through torque and rotational velocity time series

## Pros

- Full control – relation between torque and rotational velocity can be specified

## Cons

- Cost
- Complexity





# Scatter diagrams, power matrix...

- Load optimization
- Assumption on
  - max. generator capacity
  - level of active control
    - short term, wave to wave
    - longer term, sea state

Average power production estimated by multiplying (matrices)  
 $\text{Prob} \times P_{\text{wave}} \times \text{eff.}$   
(Scatter Diagram  $\times$  Power Matrix)

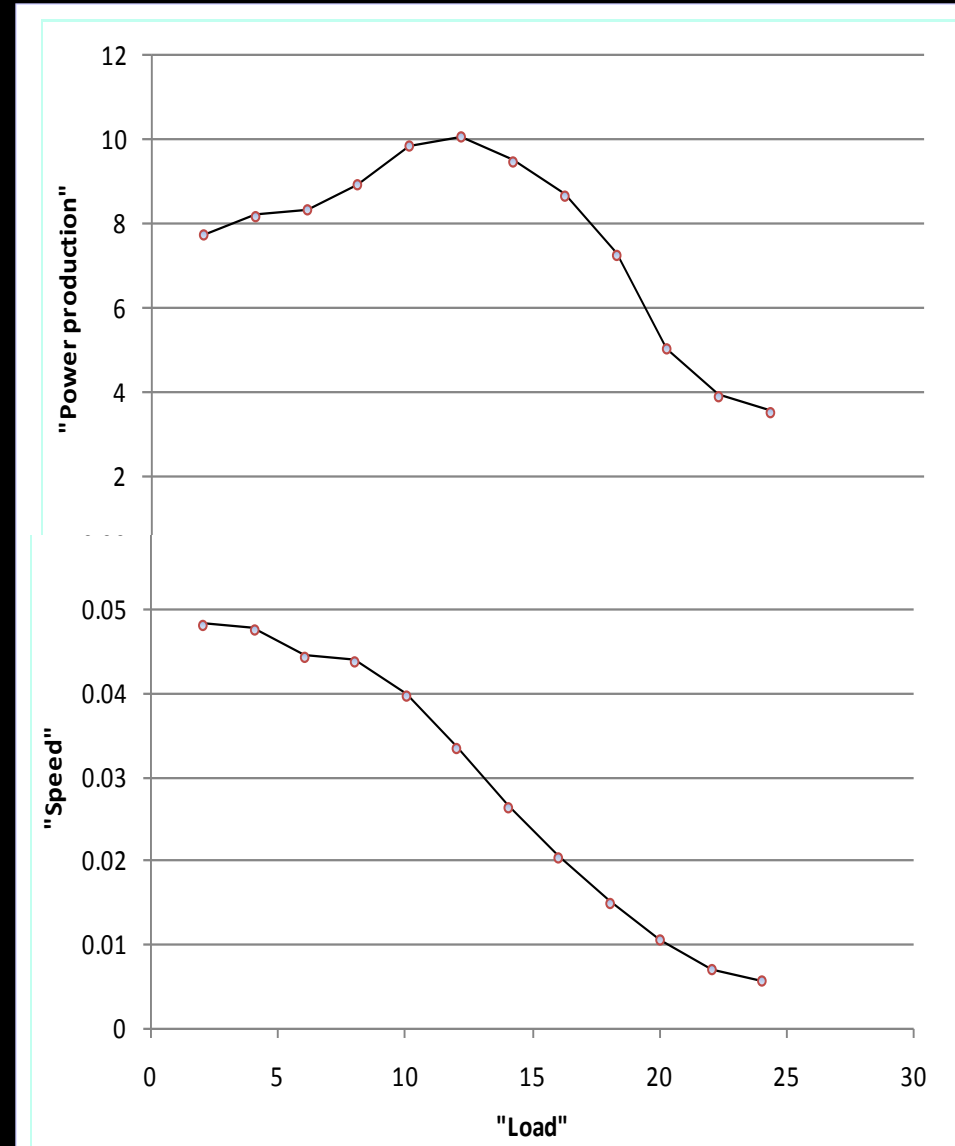
# Load optimization

Often load optimized using regular waves  
(maintaining energy contents)

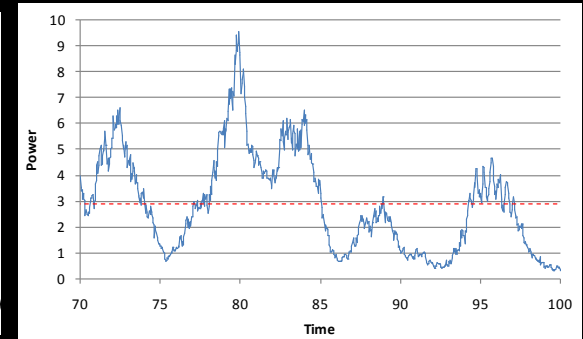
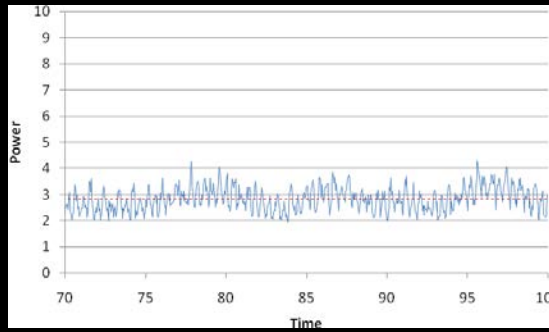
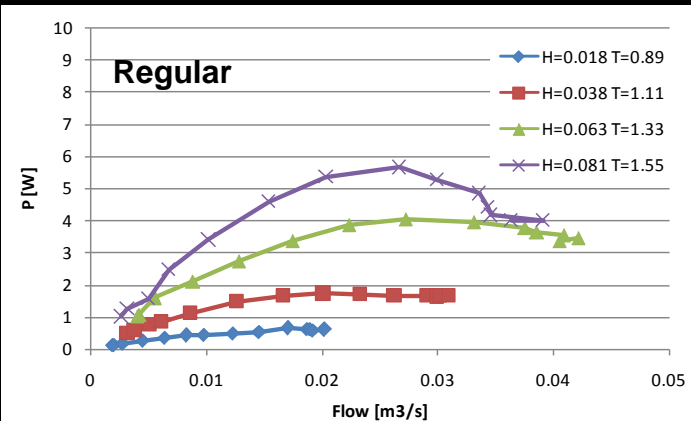
- $H = H_{m0}/\sqrt{2}$
- $T = T_p$

Optimization for each wave condition

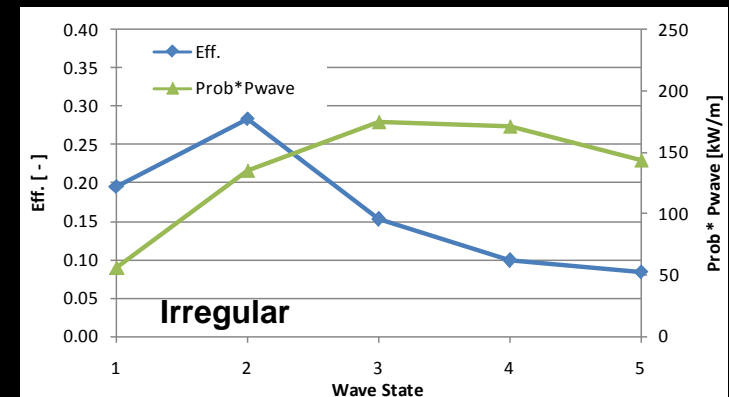
Power production measured in irregular waves using found optimal load setting  
(plus check runs on either sides)



# Estimation of yearly power production



Wave State	P <sub>wave</sub> [kW]	Prob [%]	Prob*P <sub>wave</sub> [kW]	Eff. [-]	Energy prod. [kW]	P <sub>gen</sub> [kW]
1	120	0.468	56	0.195	11	23
2	598	0.226	135	0.284	38	170
3	1616	0.108	175	0.152	27	246
4	3351	0.051	171	0.098	17	330
5	5985	0.024	144	0.084	12	505
Yearly average [kW]			680		105	
Overall eff. [-]					0.154	
Yearly prod. [MWh/y]					919	
Max. P <sub>gen</sub> [MW]						0.505
Load factor [-]						0.21



# Energy production - exercise

Find Scatter Diagram and Power Matrix for Wavestar in DropBox

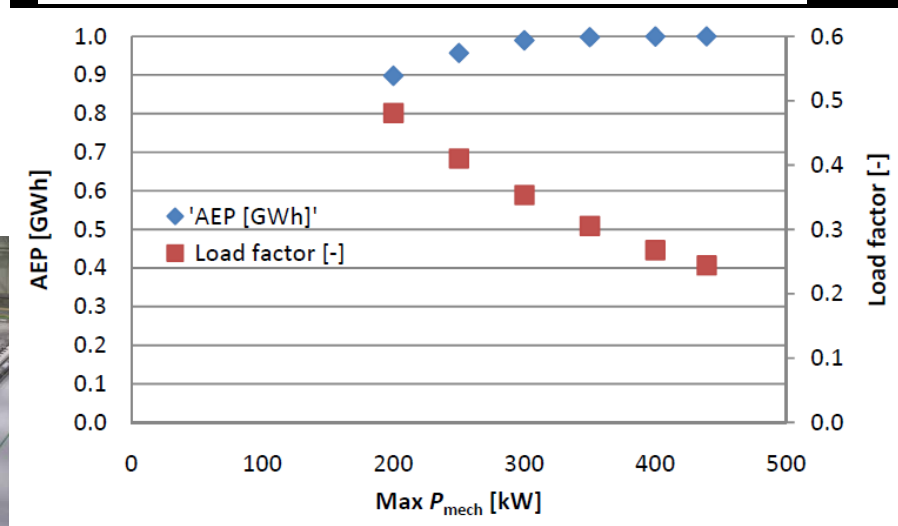
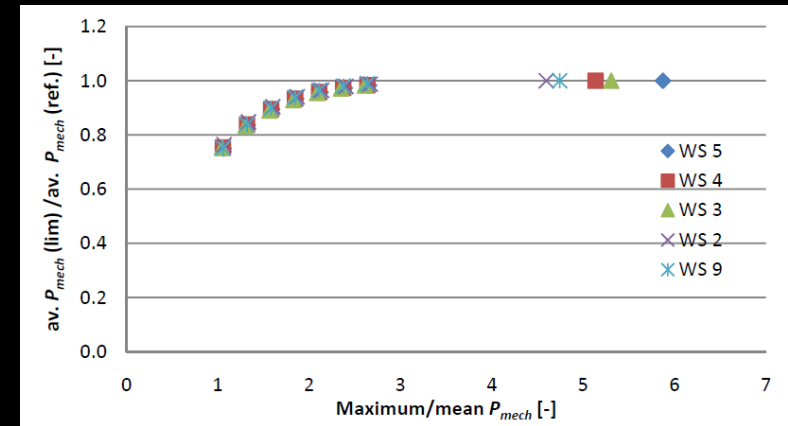
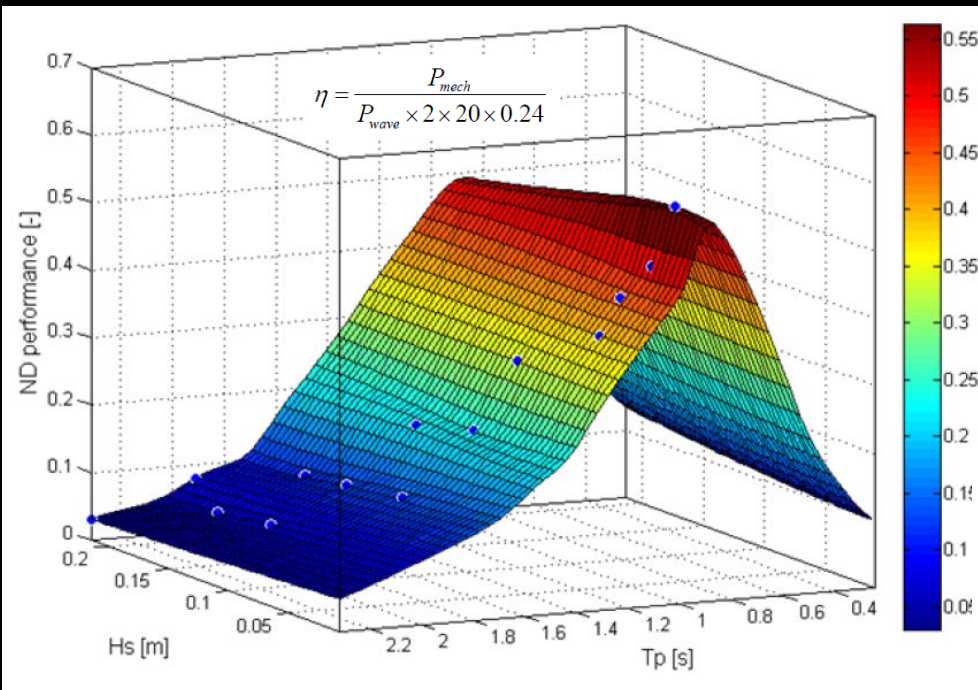
Assume the current Danish Feed-In-Tariff:

- 0.60 DKK/kWh first 10 years, 0.43 DKK/kWh hereafter

Calculate

- Annual energy production (AEP [GWh/y])
- Total expectable income during 20 years [DKK]

# Power production measurements



Weptos



# Anholt

Scaling ratio: 1.Relative to prototype 2. relative to reference	8.33		1.00		10		1.20		12		1.44		15		1.80	
Leg: 1.absolute length [m] 2.active length [m] 3.diameter [m]	63	40	2.9		76	48	3.5		91	58	4.2		114	72	5.3	
Rotor: 1.weight [ton] 2.volume [m^3] 3.width [m] 4.chord [m]	2.3	4.3	2.0	2.7	4.1	7.4	2.4	3.3	7.0	12.8	2.9	3.9	13.7	25.0	3.6	4.9
Pwave [kW/m]	0.99				0.99				0.99				0.99			
Load factor* [-] (unlimited and limited)	0.13	0.32	0.40	0.51	0.11	0.32	0.39	0.48	0.09	0.30	0.37	0.45	0.08	0.30	0.36	0.44
Maximum Pmech. [kW]	107	42	32	21	194	64	48	32	335	93	70	47	629	151	114	76
Overall $\eta$ [-]	0.18	0.17	0.16	0.14	0.22	0.21	0.20	0.16	0.27	0.25	0.23	0.19	0.35	0.32	0.28	0.23
Average Pmech [kW]	14.1	13.6	12.7	10.8	21.2	20.1	18.5	15.4	31.1	28.5	25.7	21.1	50.5	45.0	40.5	33.2
Annual Energy Production [GWh]	0.12	0.12	0.11	0.09	0.18	0.17	0.16	0.13	0.27	0.25	0.22	0.18	0.44	0.39	0.35	0.29
Relative AEP to unlimited load factor [-]	1.0	0.97	0.90	0.77	1.0	0.95	0.87	0.73	1.0	0.91	0.83	0.68	1.0	0.89	0.80	0.66
Relative AEP to reference [-]	1.00	0.97	0.90	0.77	1.51	1.43	1.31	1.09	2.21	2.02	1.83	1.50	3.59	3.20	2.88	2.36

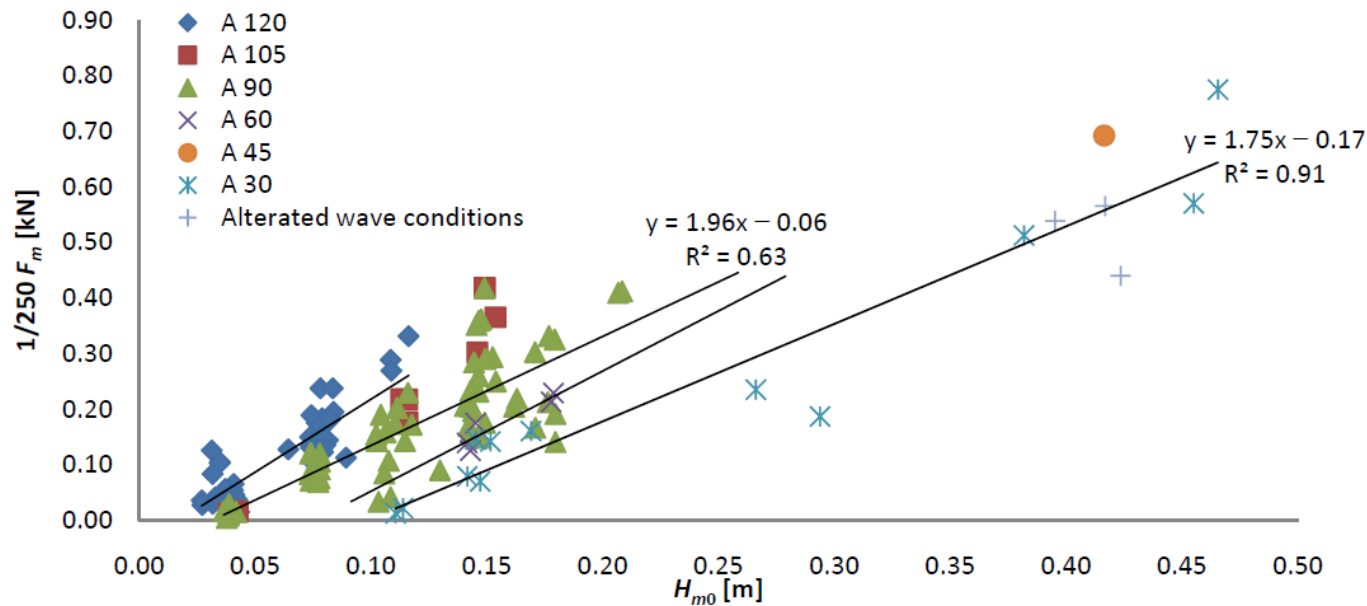
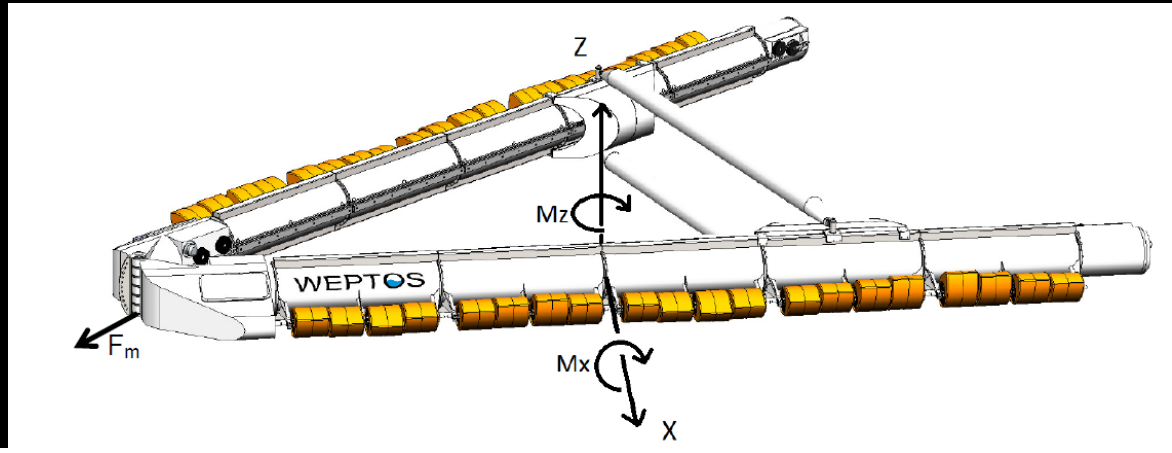
# Hanstholm (DanWEC)

Scaling ratio: 1.Relative to prototype 2. relative to reference	12		1.0		15		1.25		20		1.67		25		2.08	
Leg: 1.absolute length [m] 2.active length [m] 3.diameter [m]	91	58	4.2		114	72	5.3		152	96	7.1		190	120	8.9	
Rotor: 1.weight [ton] 2.volume [m^3] 3.width [m] 4.chord [m]	7	13	2.9	3.9	14	25	3.6	4.9	32	59	4.8	6.5	63	115.7	6.0	8.2
Pwave [kW/m]	6.1				6.1				6.1				6.1			
Load factor* [-] (unlimited and limited)	0.08	0.33	0.42	0.55	0.08	0.33	0.42	0.54	0.06	0.32	0.41	0.52	0.06	0.32	0.39	0.50
Maximum Pmech. [kW]	757	176	132	88	1454	330	247	165	3656	699	524	349	6017	1166	875	583
Overall $\eta$ [-]	0.08	0.08	0.08	0.07	0.12	0.12	0.12	0.10	0.20	0.19	0.18	0.15	0.26	0.25	0.23	0.20
Average Pmech [kW]	59	58	56	48	110	108	103	89	233	226	213	183	389	370	344	293
Annual Energy Production [GWh]	0.5	0.5	0.5	0.4	1.0	0.9	0.9	0.8	2.0	2.0	1.8	1.6	3.4	3.2	3.0	2.5
Relative AEP to unlimited load factor [-]	1.0	0.99	0.95	0.82	1.0	0.99	0.94	0.81	1.0	0.97	0.91	0.78	1.0	0.95	0.89	0.75
Relative AEP to reference [-]	1.0	0.99	0.95	0.82	1.87	1.85	1.76	1.52	3.97	3.86	3.63	3.11	6.63	6.31	5.87	4.99

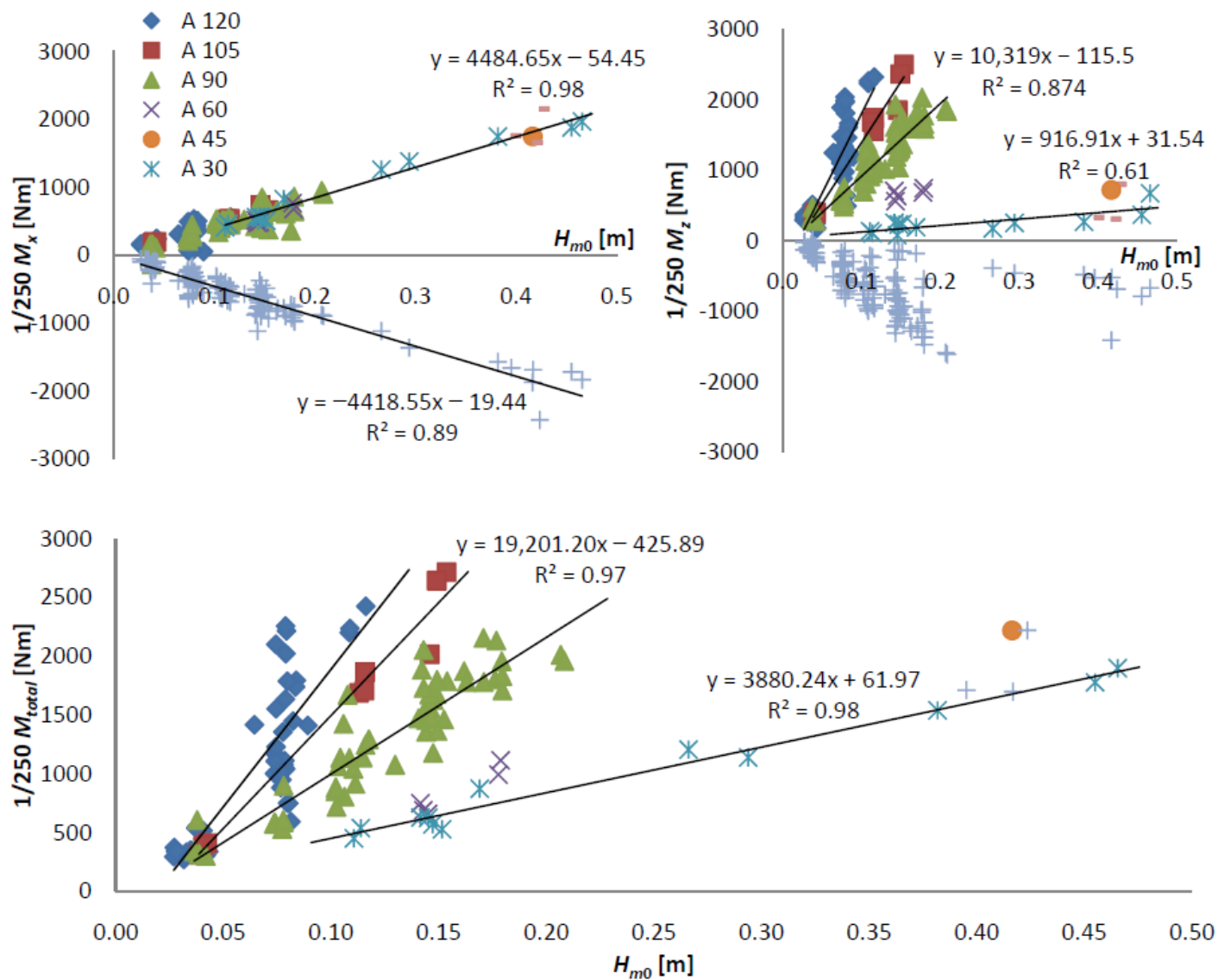
# Danish part of the North Sea

Scaling ratio: 1.Relative to prototype 2. relative to reference	23.4				25				30				35			
Leg: 1.absolute length [m] 2.active length [m] 3.diameter [m]	178	112	8.3		190	120	8.9		228	144	10.6		266	168	12.4	
Rotor: 1.weight [ton] 2.volume [m^3] 3.width [m] 4.chord [m]	52	95	5.6	7.6	63	116	6.0	8.2	110	200	7.2	9.8	174	317.6	8.4	11.4
Pwave [kW/m]	16.3				16.3				16.3				16.3			
Load factor* [-] (unlimited and limited)	0.18	0.33	0.42	0.55	0.19	0.33	0.42	0.54	0.18	0.33	0.41	0.52	0.16	0.32	0.39	0.49
Maximum Pmech. [kW]	2080	1147	860	574	2422	1368	1026	684	4126	2196	1647	1098	6627	3152	2364	1576
Overall $\eta$ [-]	0.10	0.10	0.10	0.09	0.12	0.12	0.11	0.09	0.16	0.15	0.14	0.12	0.19	0.19	0.17	0.14
Average Pmech [kW]	382	379	363	315	456	452	430	370	732	721	677	573	1051	1012	933	780
Annual Energy Production [GWh]	3.3	3.3	3.1	2.7	4.0	3.9	3.7	3.2	6.3	6.2	5.9	5.0	9.1	8.8	8.1	6.8
Relative AEP to unlimited load factor [-]	1.0	0.99	0.95	0.82	1.0	0.99	0.94	0.81	1.0	0.98	0.92	0.78	1.0	0.96	0.89	0.74
Relative AEP to reference [-]	1.00	0.99	0.95	0.82	1.19	1.18	1.12	0.97	1.91	1.89	1.77	1.50	2.75	2.65	2.44	2.04

# Loadings







# COE Calculation spreadsheet

## COE Calculation Tool

version 1.6

## Reference machine

Name of project

WEC name, project and location

Power known as:

Power matrix

Power matrix refers to:

Electrical power

Location

UK - Portland Firth

Wave: 7.1 kW/m

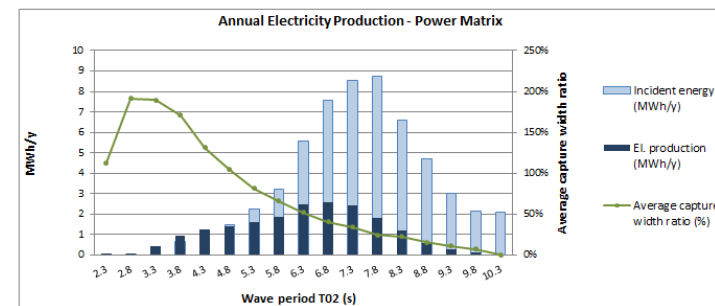
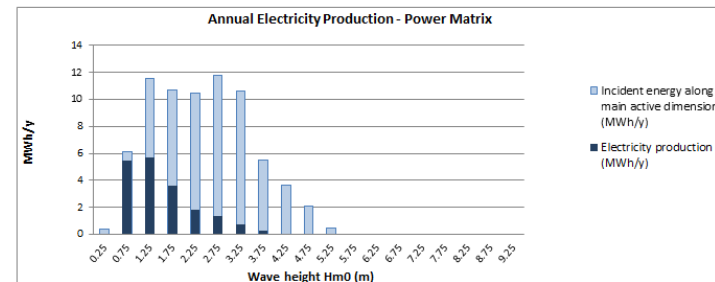
Capacity factor	41%
Annual electricity production	19 MWh/y
Average annual electricity production	2 kW
Average wave-to-wire efficiency	25%

Update and  
Show graphs

Currency	EUR	Development stage: Phase 4 / TRL 8		[-40 to 40%] uncertainty
	FIT-UK (€/MWh)	367.5	600.0	
	Total CapEx	0.25 M€	Annual OpEx	20.10 k€/y
	Payback period	Greater than project lifetime		
	Discount rate	0%	4%	8.0%
	LCOE (15 years, in €/MWh)	1933	2154	2402
	NPV (15 years, in k€)	-381.3	-347.7	-325.5

## WEC's features and performance

	Default	Enter	Used
Scale	1.00		1.00
Main active dimension		1.2	1.20 m
Secondary dimension (length/width)		3.6	3.60 m



Contact person:

Julia Fernández Chozas

coe@juliafchozas.com

+45 28 70 02 19

## Legend

	Editable cell
	Default values
	Used values

## Costs (CapEx and OpEx)

	Default	Enter	Used
Engineering and management	0.0		0 DKKx1000
Planning and consenting	0.0		0 DKKx1000
Development	54.9		55 DKKx1000
Main material	Concrete	0.8	1 DKKx1000

Standard values

3% CapEx  
1500 DKK/ton

## COE sheet

[http://vbn.aau.dk/en/publications/user-guide--coe-calculation-tool-for-wave-energy-converters\(78b135d9-ea66-43f8-959f-c799dc4df1a9\).html](http://vbn.aau.dk/en/publications/user-guide--coe-calculation-tool-for-wave-energy-converters(78b135d9-ea66-43f8-959f-c799dc4df1a9).html)

# Shortcomings of SD/PM approach

- Resolution
- Linear interpolation
- Standard spectral shape
- Constant bin size
- More dimensions (direction, water level, ...)
- Limited data sets
- See more e.g.
  - Andres Gutierrez, AD 2015, 'Finding gaps on techno-economic assessment on Wave Energy Converters: path towards commercialization'. PhD thesis, University of Cantabria
  - Lavelle, J & Kofoed, JP 2013, 'Representative spectra of the wave resource from real sea wave measurements'. in Proc. 10th EWTEC, Aalborg.
  - Kofoed, JP et al. 2013, 'A Methodology for Equitable Performance Assessment and Presentation of Wave Energy Converters Based on Sea Trials' Renewable Energy, vol 52, no. April, pp. 99-110., 10.1016/j.renene.2012.10.040

Questions - comments?

Thank you!

